

Constraining Variations in the Fine Structure Constant in the presence of Early Dark Energy

Erminia Calabrese^a, Eloisa Menegoni^a, C.J.A.P. Martins^{b,c}, Alessandro Melchiorri^a, and Graca Rocha^d

^a *Physics Department and INFN, Università di Roma “La Sapienza”, Ple Aldo Moro 2, 00185, Rome, Italy*

^b *Centro de Astrofísica, Universidade do Porto, Rua das Estrelas, 4150-762 Porto, Portugal*

^c *DAMTP, University of Cambridge, Wilberforce Road, Cambridge CB3 0WA, United Kingdom and*

^d *Jet Propulsion Laboratory, California Institute of Technology, California, USA*

We discuss present and future cosmological constraints on variations of the fine structure constant α induced by an early dark energy component having the simplest allowed (linear) coupling to electromagnetism. We find that current cosmological data show no variation of the fine structure constant at recombination respect to the present-day value, with $\alpha/\alpha_0 = 0.975 \pm 0.020$ at 95% c.l., constraining the energy density in early dark energy to $\Omega_e < 0.060$ at 95% c.l.. Moreover, we consider constraints on the parameter quantifying the strength of the coupling by the scalar field. We find that current cosmological constraints on the coupling are about 20 times weaker than those obtainable locally (which come from Equivalence Principle tests). However forthcoming or future missions, such as Planck Surveyor and CMBPol, can match and possibly even surpass the sensitivity of current local tests.

PACS numbers: 98.80.Cq, 04.50.+h, 95.35.+d, 98.70.Vc

I. INTRODUCTION

Cosmology has recently entered a precision, data-driven era. The availability of ever larger, higher-quality datasets has led to the so-called concordance model. This is a remarkably simple model (with a small number of free parameters) which provides a very good fit to the existing data (see e.g. [1–4]). However, there is a price to pay for this success: the data suggests that 96% of the contents of the universe are in a still unknown form, that so far has never been seen in a laboratory. This is often called the dark sector of the universe.

Current best estimates suggest that this dark sector is in fact a combination of two distinct components (see e.g. [6] for recent reviews). The first is called dark matter (making up about 23% of the universe) and it is clustered in large-scale structures like galaxies. The second, which has gravitational properties very similar to those of the cosmological constant first proposed by Einstein, is called dark energy and currently dominates the universe, with about 73% of its density. Understanding what constitutes this dark energy is one of the most important problems of modern cosmology. In particular, we would like to find out if it is indeed a cosmological constant, since there are many possible alternatives. These alternative models often involve scalar fields, an example of which is the Higgs field which the LHC is searching for.

There are two main differences between the cosmological constant and the models involving scalar fields (which are often collectively called dynamical dark energy models). First, in the former case the density of dark energy is a constant while in the latter the dark energy density does change. Second, the scalar fields will necessarily couple to other fields (unless they are prevented from doing so by symmetry principles) and thus can lead to further distinguishing features [7] such as variations of nature’s fundamental couplings. A case in point is the

coupling of the scalar field to the electromagnetic sector of the model, which will lead to spacetime variations of the fine-structure constant α .

One way to distinguish a cosmological constant from dynamical dark energy is therefore to find several independent ways to measure the dark energy density (or its equation of state $w = p/\rho$) at several epochs in the universe, while at the same time searching for variations of α or other dimensionless couplings [8].

Cosmic Microwave Background Anisotropies (CMB hereafter) have provided in the past years a powerful method to constrain variations in the fine structure constant in the early universe, at the epoch of recombination (see e.g. [9–15]) at the level of $\sim 1\%$. In the most recent analysis, parametrizing a variation in the fine structure constant as α/α_0 , where $\alpha_0 = 1/137.03599907$ is the standard (local) value and α is the value during the recombination process, the authors of [14] used the five year WMAP data, finding the constraint 0.987 ± 0.012 at 68% c.l..

The presence of a scalar field at recombination could induce variations in the fine structure constant. While the effects of a cosmological constant at recombination are completely negligible, dynamical scalar fields could track the dominant energy component, be present at recombination and induce variations in α if coupled to the electromagnetic sector. It is therefore timely to check for variations of the fine structure constant in cosmological data allowing at the same time the presence of an “early” dark energy component at recombination. All recent cosmological constraints on α have indeed been obtained under the assumption of a cosmological constant or of a dark energy component with constant equation of state w ([16]), i.e. in the case of a negligible dark component at recombination. Clearly, if a dark energy is present in the early universe, degeneracies between the parameters may arise and change the current results. Moreover, in

the past year, a significant experimental progress in determining the CMB angular power spectrum has been made, most notably from the Atacama Cosmology Telescope (ACT) ([2]). This new data, as we will see in the next sections, substantially improve previous constraints on α .

In this paper we indeed follow this way of reasoning and we produce new constraints on variation of α allowing at the same time for the presence of dark energy at recombination. In order to be as general as possible, we describe the scalar field adopting a phenomenological approach, considering an early dark energy model (hereafter, EDE) as discussed in [17]. We consider a class of models where the link between the dark energy and electromagnetic sectors is explicit. Specifically we discuss present and future constraints on EDE models having the simplest allowed (linear) coupling to electromagnetism.

Our paper is therefore structured as follows: in the next Section we briefly describe the early dark energy model considered and its coupling to electromagnetic sector. In Section III we present the data analysis method used while in Section IV we discuss our results.

II. EARLY DARK ENERGY AND THE ELECTROMAGNETIC SECTOR

As discussed in the previous section we aim to place constraints on variations of the fine structure constant with a non-negligible scalar field at recombination. We describe the scalar field with a EDE model [17] where the dark energy density parameter and equation of state are parametrized in the following way :

$$\Omega_{\text{de}}(a) = \frac{\Omega_{\text{de}}^0 - \Omega_{\text{e}}(1 - a^{-3w_0})}{\Omega_{\text{de}}^0 + \Omega_{\text{m}}^0 a^{3w_0}} + \Omega_{\text{e}}(1 - a^{-3w_0}) \quad (1)$$

$$w(a) = -\frac{1}{3[1 - \Omega_{\text{de}}(a)]} \frac{d \ln \Omega_{\text{de}}(a)}{d \ln a} + \frac{a_{\text{eq}}}{3(a + a_{\text{eq}})} \quad (2)$$

where a_{eq} is the scale factor at matter-radiation equality and Ω_{de}^0 and Ω_{m}^0 are the current dark energy and matter density, respectively. A flat Universe is assumed so $\Omega_{\text{m}}^0 + \Omega_{\text{de}}^0 = 1$ and the present value for the equation of state is obtained from demanding $w(a=1) = w_0$. The energy density $\Omega_{\text{de}}(a)$ has a scaling behaviour evolving with time and going to a finite constant Ω_{e} in the past.

The dark energy equation of state $w(a)$ follows the behaviours of the dominant component at each cosmic time : $w \approx 1/3$ during radiation domination, $w \approx 0$ during matter domination, and $w \approx w_0$ in recent epochs as in a cosmological constant era. We add dark energy perturbations as in [18] by considering the EDE clustering properties through the effective sound speed $c_s^2 = \delta p / \delta \rho$ and a viscosity parameter c_{vis}^2 accounting for the presence of anisotropic stresses. In the present analysis we assume these clustering parameters as constant with $c_s^2 = 1$ and $c_{\text{vis}}^2 = 0$ as expected in the case of a scalar field. For

simplicity we also fix $w_0 = -1$ since this value is well constrained by low redshift data.

In any realistic dynamical scalar field scenario, the scalar field should be coupled to the rest of the model, unless one postulates a (yet unknown) symmetry to suppress the coupling. We are presently interested in the coupling between the scalar field and electromagnetism, which we take to be of the form :

$$\mathcal{L}_{\phi F} = -\frac{1}{4} B_F(\phi) F_{\mu\nu} F^{\mu\nu} \quad (3)$$

where the gauge kinetic function $B_F(\phi)$ is linear,

$$B_F(\phi) = 1 - \zeta \kappa (\phi - \phi_0) \quad (4)$$

and $\kappa^2 = 8\pi G$; ζ is therefore the relevant coupling, and among other things it is related to the amount of equivalence principle violations. Constraints on this coupling are tight at low redshift; conservatively we have [19, 20]:

$$|\zeta_{\text{local}}| < 10^{-3}. \quad (5)$$

In this work we will derive an analogous but independent constraint coming from the CMB.

This form of the gauge kinetic function can be seen as the first term of a Taylor expansion, and given the tight low-redshift constraints on varying couplings it is a good approximation for a slowly varying field at low redshift. Here we are extending it all the way to the CMB epoch. In this case, how good an approximation this is will be more model-dependent. However, given that a purely phenomenological parametrization for EDE is already being assumed, this choice of parametrization for the gauge kinetic function should be quite adequate. We will comment further on these choices at the end of the paper.

This being said, the evolution of alpha is given by :

$$\frac{\Delta \alpha}{\alpha} \equiv \frac{\alpha - \alpha_0}{\alpha_0} = \zeta \kappa (\phi - \phi_0), \quad (6)$$

and since the evolution of the scalar field can be expressed in terms of the dark energy properties Ω_{de} and w as [8, 21]:

$$w = -1 + \frac{(\kappa \phi')^2}{3\Omega_{\text{de}}}, \quad (7)$$

(where the prime denotes the derivative with respect to the logarithm of the scale factor) we finally obtain the following explicit relation specifying the evolution of the fine structure constant in the early dark energy class of models :

$$\alpha/\alpha_0(a) = 1 - \zeta \int_a^{a_0} \sqrt{3\Omega_{\text{de}}(a)(1 + w(a))} d \ln a. \quad (8)$$

As expected the magnitude of the variation is controlled by the strength of the coupling ζ .

III. ANALYSIS METHOD

We have modified the CAMB [22] code for early dark energy as in [18] and we include variations in the fine structure constant in the recombination process using the method adopted in [9] and modifying the publicly available RECFAST [23] routine.

We constrain variation in the fine structure constant α/α_0 and Ω_e by a COSMOMC analysis of the most recent CMB data. The analysis method we adopt is based on the publicly available Markov Chain Monte Carlo package `cosmomc` [24] with a convergence diagnostics done through the Gelman and Rubin statistics.

We sample the following eight-dimensional set of cosmological parameters, adopting flat priors on them: the baryon and cold dark matter densities ω_b and ω_c , the Hubble parameter H_0 , the scalar spectral index n_s , the overall normalization of the spectrum A_s at $k = 0.05 \text{ Mpc}^{-1}$, the optical depth to reionization, τ , the ratio of the values of the fine structure constant then and now α/α_0 and, finally, the primordial amount of early dark energy Ω_e . Furthermore, we consider purely adiabatic initial conditions and we impose spatial flatness.

We consider WMAP7 [1] and ACT [2] as CMB datasets and we analyze datasets out to $l_{max} = 2500$. In order to investigate the impact of the recent ACT dataset alone we perform two different analysis, WMAP7 and WMAP7+ACT as CMB probes. For the ACT dataset we moreover consider two extra parameters accounting for the Poisson and clustering point source foreground components. We also include informations on dark energy from Baryonic Acoustic Oscillations (BAO) in galaxy surveys [3], and finally we impose a prior on the Hubble parameter based on the Hubble Space Telescope observations [4]. More recently, new and improved constraints on the Hubble parameter have been reported in [5] and we also perform some analyses considering this new more stringent prior referring to it as HST2.

IV. COSMOLOGY MEASUREMENTS OF α , Ω_e AND ζ

A. Constraints from current data

In Table I we report the constraints on the α/α_0 and Ω_e parameters obtained from the COSMOMC analysis, using the different combinations of datasets described in the previous section. Notice the significant improvements on both parameters provided by the small-scale ACT data. As expected, because of the correlation between α and H_0 (see e.g. [14]), we found an improvement in the constraint on α of about 15% when HST2 is considered. However, when also ACT and BAO are added, the degeneracy is broken and we do not have any relevant contribution from HST2.

In Figure 1 we show the 68% and 95% c.l. constraints on the α/α_0 vs Ω_e plane for different datasets. As we can

| Datasets | α/α_0 | Ω_e | ζ |
|--------------------|-------------------|------------|-----------|
| WMAP7+HST | 0.963 ± 0.044 | < 0.064 | < 0.047 |
| WMAP7+HST2 | 0.960 ± 0.040 | < 0.070 | < 0.047 |
| WMAP7+ACT+HST | 0.975 ± 0.020 | < 0.060 | < 0.031 |
| WMAP7+ACT+HST+BAO | 0.986 ± 0.018 | < 0.050 | < 0.025 |
| WMAP7+ACT+HST2+BAO | 0.986 ± 0.016 | < 0.050 | < 0.021 |

TABLE I: Limits at 95% c.l. on α/α_0 , Ω_e and the coupling ζ from the MCMC analyses.

see, there is no strong degeneracy between Ω_e and the fine structure constant and the cosmological data can be used to put strong limits on both quantities.

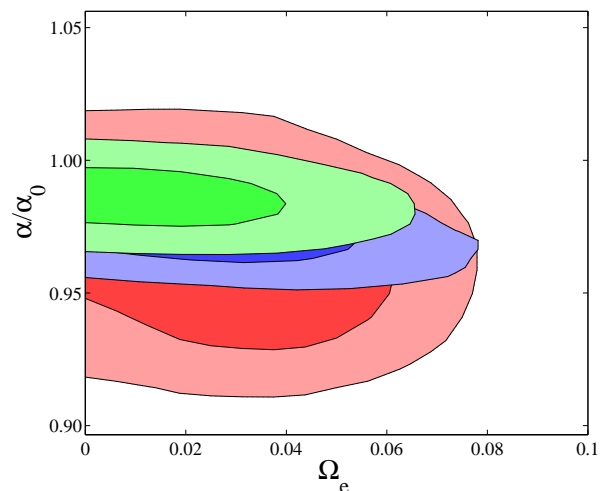


FIG. 1: 68% and 95% c.l. constraints on the α/α_0 vs Ω_e plane in the case of WMAP7+HST (red contours) compared with WMAP7+ACT+HST (blue contours) and WMAP7+ACT+BAO+HST (green contours).

We can therefore consider the value of the coupling parameter at decoupling:

$$\zeta = (1 - \alpha/\alpha_0) / \int_{a_{dec}}^{a_0} \sqrt{3\Omega_{de}(a)(1+w(a))} d \ln a \quad (9)$$

and use the constraints on Ω_e and α/α_0 obtained in our analysis to constrain variations in ζ . In Table I we report these constraints for the different analysis while Figure 2 shows the degeneracy between α/α_0 and ζ .

Although the current constraints are 20-40 times weaker than the ones that can be obtained from weak

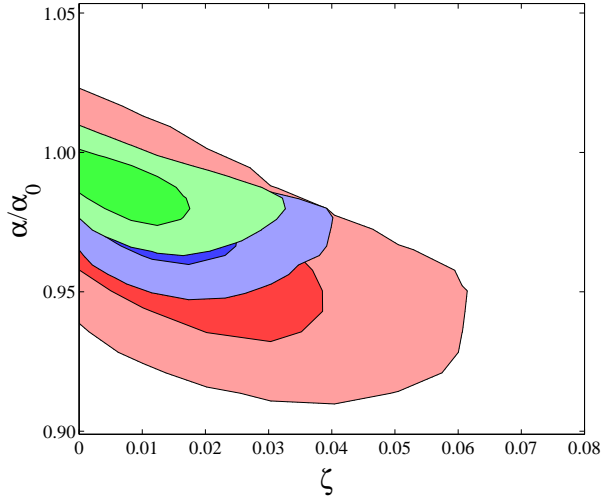


FIG. 2: 68% and 95% c.l. constraints on the α/α_0 vs ζ plane in the case of WMAP7+HST (red contours) compared with WMAP7+ACT+HST (blue contours) and WMAP7+ACT+BAO+HST (green contours).

equivalence principle tests (cf. Eqn. 5), it's important to keep in mind that our constraints are obtained on completely different scales, cosmological ones, as opposed to laboratory ones. So a discrepancy of less than two orders of magnitude is actually impressive.

To put this in context, in the case of the Eddington parameter γ , the difference in sensitivity between cosmological measurements (obtained from lensing [25], thus on kiloparsec scales) and solar system ones (from the Cassini bound [26], effectively on 10^{-4} parsec scales) is more than three orders of magnitude. This difference testifies to the exquisite sensitivity of current CMB datasets and of course the situation will improve with forthcoming datasets, as we now discuss.

B. Forecasts for Planck and CMBPol

To evaluate future sensitivity to these parameters from CMB we consider noise properties consistent with the Planck [27] and CMBPol [28] experiments (see Table II for specifications).

We consider for each channel a detector noise of $w^{-1} = (\theta\sigma)^2$, where θ is the Full-Width at Half-Maximum (FWHM) of the beam assuming a Gaussian profile and σ is the temperature/polarization sensitivity $\Delta T/\Delta P$ (see Tab. II). We therefore derive a noise spectrum given by:

$$N_\ell = w^{-1} \exp(\ell(\ell+1)/\ell_b^2), \quad (10)$$

where ℓ_b is $\ell_b \equiv \sqrt{8 \ln 2}/\theta$.

We then perform a Fisher matrix analysis [29] to estimate the $1 - \sigma$ error for each parameter. We assume a Λ CDM fiducial model with the following parameters: $\Omega_b h^2 = 0.02258$, $\Omega_c h^2 = 0.1109$, $\tau = 0.088$,

| Experiment | Channel | FWHM | ΔT | ΔP |
|------------------|---------|-------|------------|------------|
| Planck | 70 | 14' | 12.8 | 18.3 |
| | 100 | 10' | 6.8 | 10.9 |
| | 143 | 7.1' | 6.0 | 11.4 |
| CMBPol | 70 | 12.0' | 0.148 | 0.209 |
| | 100 | 8.4' | 0.151 | 0.214 |
| | 150 | 5.6' | 0.177 | 0.250 |
| $f_{sky} = 0.85$ | | | | |

TABLE II: Planck and CMBPol experimental specifications. Channel frequency is given in GHz, Full-Width at Half-Maximum (FWHM) in arc-minutes, and the temperature and polarization sensitivity per pixel in μK .

$H_0 = 71$ km/s/Mpc, $n_s = 0.963$ plus the EDE parameters that we fix to : $w_0 = -0.90$, $\Omega_e = 0.03$, $c_s^2 = 1$, $c_{vis}^2 = 0$ and $\alpha/\alpha_0 = 1$.

Results for the parameters of direct interest are shown in Table III. Forecasts for the fine-structure constant are comparable to those of our earlier work [10], when one allows for the slightly different assumptions and fiducial model. More interestingly, we see that Planck can constrain the scalar field coupling ζ with an accuracy comparable to that of current local bounds, while CMBPol can do about five times better. However, it should also be pointed out that local bounds are expected to improve with the advent of satellite-based tests of the equivalence principle.

| Experiment | σ_{α/α_0} | σ_{Ω_e} | σ_ζ |
|------------|----------------------------|---------------------|----------------|
| Planck | 0.0012 | 0.0036 | < 0.0012 |
| CMBPol | 0.00025 | 0.0015 | < 0.00022 |

TABLE III: Fisher matrix errors at 68% c.l. on α/α_0 and Ω_e and upper bounds at 95% on coupling ζ from Planck and CMBPol.

We report in Figure 3 the 2-dimensional contour plots in the $\alpha/\alpha_0 - \Omega_e$ plane showing the 1 and $2 - \sigma$ regions for Planck with solid lines and CMBPol with dashed lines. The effect of the better polarization data in further constraining α is quite noticeable.

V. CONCLUSIONS

We have discussed present constraints on variations of the fine structure constant α in the context of phenomenological class of early dark energy where the putative dynamical scalar field is coupled to the electro-

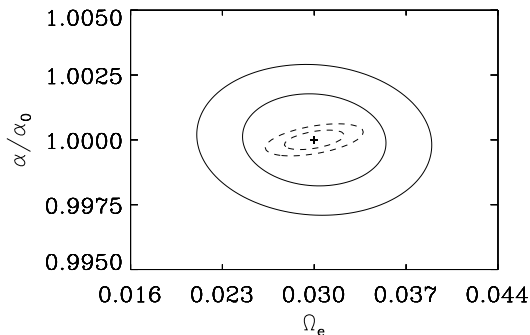


FIG. 3: 68% and 95% c.l. estimated constraints on the α/α_0 vs Ω_e plane from Planck (solid lines) and CMBPol (dashed lines).

magnetic sector of the theory through the simplest allowed (linear) coupling. We have found no significant correlation between α/α_0 and the early dark energy density parameter Ω_e , providing the constraints $\alpha/\alpha_0 = 0.975 \pm 0.020$ and $\Omega_e < 0.060$ at 95% c.l. The constraints on α are significantly improved with respect to the WMAP five-years constraint [14], thanks to the new ACT data.

Moreover we have used the CMB and other cosmological datasets to also constrain the dimensionless parameter quantifying the strength of the scalar field coupling, ζ , at the epoch of decoupling, in addition to constraining α itself. While the current data only allowed us to obtain a constraint on ζ that is about 20 times weaker than those obtainable locally (which come from Equivalence Principle tests), we emphasize that the two constraints are independent. Moreover, forthcoming or future missions, such as Planck Surveyor and CMBPol, can match

and possibly even surpass the sensitivity of current local tests.

Admittedly the toy model which we have studied may well be too simplistic, and we are currently investigating how sensitive our results are to our choice of parametrization. Nevertheless, we emphasize that the model has the clear virtue of being predictive enough to be confirmed or ruled out by forthcoming experiments. This will require a combination of cosmological datasets (Planck being the best example) and better low-redshift constraints on variations of α , which will soon be available.

Finally, this work is an example of how one can use the early universe as a laboratory in which to directly probe fundamental physics scenarios, in ways that will complement and enhance local, small-scale tests. Moreover, further avenues for searching for new physics will soon be available. Now that experiments such as MICROSCOPE[30] and ACES [31] are getting ready to perform Equivalence Principle tests in microgravity, it is encouraging that there are good prospects for carrying out analogous tests on astrophysical and cosmological scales. Synergies between local experiments and cosmological observations will soon allow us to probe unexplored aspects of gravity and fundamental physics. We will revisit these issues in future work.

Acknowledgments

This work is supported by PRIN-INAF, "Astronomy probes fundamental physics". The work of C.M. is funded by a Ciência2007 Research Contract, funded by FCT/MCTES (Portugal) and POPH/FSE (EC). C.M. and G.R. also acknowledge additional support from project PTDC/FIS/111725/2009 from FCT, Portugal. We thank Eric V. Linder for useful comments.

-
- [1] E. Komatsu *et al.*, arXiv:1001.4538 [astro-ph.CO].
 - [2] J. Dunkley *et al.*, arXiv:1009.0866 [astro-ph.CO].
 - [3] B. A. Reid *et al.* [SDSS Collaboration], Mon. Not. Roy. Astron. Soc. **401** (2010) 2148 [arXiv:0907.1660 [astro-ph.CO]].
 - [4] A. G. Riess *et al.*, Astrophys. J. **699**, 539 (2009) [arXiv:0905.0695 [astro-ph.CO]].
 - [5] A. G. Riess *et al.*, Astrophys. J. **730** (2011) 119 [arXiv:1103.2976 [astro-ph.CO]].
 - [6] E. J. Copeland, M. Sami, S. Tsujikawa, Int. J. Mod. Phys. **D15** (2006) 1753-1936. [hep-th/0603057]; A. Silvestri, M. Trodden, Rept. Prog. Phys. **72** (2009) 096901. [arXiv:0904.0024 [astro-ph.CO]]; R. R. Caldwell, M. Kamionkowski, Ann. Rev. Nucl. Part. Sci. **59**, 397-429 (2009). [arXiv:0903.0866 [astro-ph.CO]]; S. Tsujikawa, [arXiv:1004.1493 [astro-ph.CO]].
 - [7] S. M. Carroll, Phys. Rev. Lett. **81** (1998) 3067-3070. [astro-ph/9806099].
 - [8] P. P. Avelino, C. J. A. P. Martins, N. J. Nunes, K. A. Olive, Phys. Rev. **D74** (2006) 083508. [astro-ph/0605690].
 - [9] P. P. Avelino *et al.*, Phys. Rev. D **64** (2001) 103505 [arXiv:astro-ph/0102144]; C. J. A. Martins, A. Melchiorri, R. Trotta, R. Bean, G. Rocha, P. P. Avelino and P. T. P. Viana, Phys. Rev. D **66** (2002) 023505 [arXiv:astro-ph/0203149].
 - [10] C. J. A. Martins, A. Melchiorri, G. Rocha, R. Trotta, P. P. Avelino and P. T. P. Viana, Phys. Lett. B **585**, 29 (2004) [arXiv:astro-ph/0302295]; G. Rocha, R. Trotta, C. J. A. Martins, A. Melchiorri, P. P. Avelino, R. Bean and P. T. P. Viana, Mon. Not. Roy. Astron. Soc. **352**, 20 (2004) [arXiv:astro-ph/0309211].
 - [11] K. Ichikawa, T. Kanzaki and M. Kawasaki, Phys. Rev. D **74** (2006) 023515 [arXiv:astro-ph/0602577].
 - [12] P. Stefanescu, New Astron. **12** (2007) 635 [arXiv:0707.0190 [astro-ph]].
 - [13] M. Nakashima, R. Nagata and J. Yokoyama, Prog. Theor. Phys. **120** (2008) 1207 [arXiv:0810.1098 [astro-

- ph]].
- [14] E. Menegoni, S. Galli, J. G. Bartlett, C. J. A. Martins and A. Melchiorri, Phys. Rev. D **80** (2009) 087302 [arXiv:0909.3584 [astro-ph.CO]];
 - [15] C. G. Scoccola, S. .J. Landau, H. Vucetich, Phys. Lett. **B669** (2008) 212-216. [arXiv:0809.5028 [astro-ph]]; S. .J. Landau, C. G. Scoccola, [arXiv:1002.1603 [astro-ph.CO]].
 - [16] E. Menegoni et al., International Journal of Modern Physics D, Volume 19, Issue 04, pp. 507-512 (2010).
 - [17] M. Doran and G. Robbers, JCAP **0606** (2006) 026 [arXiv:astro-ph/0601544].
 - [18] E. Calabrese, R. de Putter, D. Huterer, E. V. Linder and A. Melchiorri, arXiv:1010.5612 [astro-ph.CO].
 - [19] K. A. Olive, M. Pospelov, Phys. Rev. **D65** (2002) 085044. [hep-ph/0110377].
 - [20] G. R. Dvali, M. Zaldarriaga, Phys. Rev. Lett. **88** (2002) 091303. [hep-ph/0108217].
 - [21] N. J. Nunes, T. Dent, C. J. A. P. Martins, G. Robbers, Mem. Soc. Astron. It. **80** (2009) 785. [arXiv:0910.4935 [astro-ph.CO]].
 - [22] A. Lewis, A. Challinor and A. Lasenby, Astrophys. J. **538** (2000) 473 [arXiv:astro-ph/9911177].
 - [23] W. Y. Wong, A. Moss and D. Scott, arXiv:0711.1357 [astro-ph].
 - [24] A. Lewis and S. Bridle, Phys. Rev. D **66**, 103511 (2002) (Available from <http://cosmologist.info>.)
 - [25] J. Schwab, A. S. Bolton, S. A. Rappaport, Astrophys. J. **708** (2010) 750-757. [arXiv:0907.4992 [astro-ph.CO]].
 - [26] B. Bertotti, L. Iess, P. Tortora, Nature **425** (2003) 374.
 - [27] [Planck Collaboration], arXiv:astro-ph/0604069.
 - [28] J. Bock *et al.* [EPIC Collaboration], arXiv:0906.1188 [astro-ph.CO].
 - [29] J. R. Bond, G. Efstathiou and M. Tegmark, Mon. Not. Roy. Astron. Soc. **291** (1997) L33 [arXiv:astro-ph/9702100].
 - [30] P. Touboul, G. Metris, A. Robert, A. Levy and G. Campergue 38th COSPAR Scientific Assembly **38** (2010) 3733; <http://smc.cnes.fr/MICROSCOPE/Fr/>
 - [31] P. Wolf, C. Salomon and S. Reynaud, IAU Symposium **261** (2010) 377-389; http://www.esa.int/SPECIALS/HSF_Research/SEMJSK0YDUF_0.html